VPM's
DR VN BRIMS, Thane
Programme: PGDM (2016-18)
First Trimester Examination October 2016

| Subject | Quantitative Techniques - I |  |  |
| :--- | :--- | :--- | :--- |
| Roll No. |  | Marks | 60 Marks |
| Total No. of Questions | 7 | Duration | 3 Hours |
| Total No. of printed pages |  | Date | 6.10.2016 |

Note: Q1 is compulsory and solve any FOUR from the remaining SIX questions.
Q1) 20 Marks (Compulsory)

1. Find the missing frequencies in the following distribution, for which it is known that median $=48.25$ \& mode $=44$ ( $\mathbf{1 0}$ Marks)

| Class Intervals | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Freq. | 3 | 7 | $?$ | $?$ | $?$ | 20 | 16 | 4 | 150 |

2. Answer following questions: ( $\mathbf{1 0}$ Marks)
3. The range of a data set is defined as the difference between the mean and the median. Answer true or false.
4. Standard deviation is the square of the variance. Answer true or false.
5. The time between successive arrivals of customers, Y , at a department store is an example of a continuous random variable. Answer true or false
6. Sampling error occurs when the sample is not representative of the population. Answer true or false
7. The standard error of the estimate is computed by dividing SSE by the degrees of freedom of error and then taking the square root. Answer true or false
8. In the distribution of a set of grouped data, a running total of the frequencies through the classes is given by the $\qquad$ .
a) relative frequency
b) cumulative frequency
c) class midpoint
d) median class frequency
e) modal class frequency
9. If the standard deviation of a population is 9 , the population variance is $\qquad$ .
a) 3
b) 9
c) 21
d) 27
e) 81
10. If the occurrence of one event precludes the occurrence of another other event, then the two events are $\qquad$ .
a) collectively exhaustive
b) non interacting
c) mutually exclusive
d) independent
e) joint events
11. A graphical mechanism for examining the relationship between two numerical variables is called a $\qquad$ .
a) cause-and-effect diagram
b) pie chart
c) stem and leaf plot
d) scatter plot
e) dot plot
12. In the regression equation $Y_{c}=\mathrm{a}+\mathrm{bX}$, the variable Y is the independent variable. Answer true or false
a) Obtain the 'less than' \& 'More than' cumulative frequencies from the following information

| Salary (thousand Rs.) | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ | $100-110$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of graduates freq. | 6 | 18 | 30 | 24 | 18 | 15 | 9 |

b) Salary distribution of supervisors in a company is given below. The total salary of the three supervisors in the group ' 2800 \& over' is known to be equal to Rs. 12600 . You are required to compute the mean weekly salary of supervisors.

| Salary in Rupees | No. of supervisors |
| :---: | :---: |
| $2400-2450$ | 3 |
| $2450-2500$ | 8 |
| $2500-2600$ | 12 |
| $2600-2700$ | 10 |
| $2700-2800$ | 14 |
| $2800 \&$ over | 3 |

c) A sample of 400 bulbs was put to test to find out their burning life. The results of the test are given below:

| Life (in hours) | No. of bulbs |
| :---: | :---: |
| $1600-1800$ | 14 |
| $1800-2000$ | 46 |
| $2000-2200$ | 60 |
| $2200-2400$ | 73 |
| $2400-2600$ | 68 |
| $2600-2800$ | 62 |
| $2800-3000$ | 48 |
| $3000-3200$ | 23 |
| $3200-3400$ | 6 |

Find from the given information
i. Mean life of the bulbs
ii. Standard deviation

Q3) Any two from (a) or (b) or (c) $\qquad$ (5x2) = 10 Marks
a) From the data given below, calculate the probability that an employee chosen randomly is a female or a rank 2 employee

|  | Rank |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Gender | R1 | R2 | R3 | Total |
| Male | 30 | 80 | 90 | 200 |
| Female | 20 | 40 | 40 | 100 |
| Total | 50 | 120 | 130 | 300 |

b) A variable x is normally distributed with $\mu=120 \& \sigma=10$. Find
i. $\quad \mathrm{P}(\mathrm{x}>135)$
ii. $\quad \mathrm{P}(110<\mathrm{x}<135)$
c) Find the Karl Pearson's co-efficient of correlation between age \& playing habits of the following students \& also comment on the results..

| Age of players | 16 | 17 | 18 | 19 | 20 | 21 | 22 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of students | 2500 | 2000 | 1800 | 1500 | 1200 | 1000 | 400 |
| Regular players | 2250 | 1700 | 1260 | 900 | 480 | 180 | 60 |

Q4) Any two from (a) or (b) or (c) ——— (5x2) $=10$ Marks
a) Calculate mean deviation about i) mean \& ii) median for distribution.

| Marks | No. <br> Students |
| :---: | :---: |
| $20-30$ | 4 |
| $30-40$ | 12 |
| $40-50$ | 18 |
| $50-60$ | 28 |
| $60-70$ | 19 |
| $70-80$ | 14 |
| $80-90$ | 5 |

b) Calculate the two regression coefficients \& comment on the results.

| Test Scores X | 54 | 60 | 63 | 66 | 81 | 81 | 84 | 87 | 87 | 87 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| Sales Y | 26 | 30 | 32 | 31 | 31 | 34 | 38 | 33 | 39 | 36 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

c) Calculate 4-monthly moving averages as forecasts for following data:

| Month | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Demand | 280 | 288 | 266 | 295 | 302 | 310 | 303 | 328 | 309 | 315 | 320 | 332 | 310 | 308 | 320 |

Q5) Any two from (a) or (b) or (c) ———(5x2) $=10$ Marks
a) A consumer's group is suspicious about the weight of certain brand of cereal for which the boxes are labeled as containing 12 ounces. A random sample of 50 boxes yields an average weight of 11.6 ounces with a standard deviation of 1.68 ounces. Test the hypothesis that population mean weight is 12 ounces, at the 0.05 level of significance. Calculate the p -value.
b) Develop a stem-and-leaf plot for the data.

| 25 | 31 | 20 | 32 | 13 |
| :--- | :--- | :--- | :--- | :--- |
| 14 | 43 | 02 | 57 | 23 |
| 36 | 32 | 33 | 32 | 44 |
| 32 | 52 | 44 | 51 | 45 |

c) A pack contains 30 tickets numbered consecutively from 1 to 30 . A ticket is chosen at random from this. Find the chance that the number on this would be
i. A multiple of 6 or 7
ii. A multiple of 3 or 5

Q6) Any two from (a) or (b) or (c) ——— (5x2) $=10$ Marks
a) Calculation of median \& Quartiles

| Marks | $\mathbf{f}$ | cf |
| :--- | :--- | :--- |
| $10-20$ | 62 | 62 |
| $20-30$ | 128 | 190 |
| $30-40$ | 240 | 430 |
| $40-50$ | 95 | 525 |
| $50-60$ | 75 | 600 |

b) BSES uses a sample survey to determine the average consumption per month. They survey 200 households \& find that the average electricity consumed is 9.5 units the standard deviation is 2.1. Set up the confidence limits on the basis of $95 \%$ level of confidence as well as $99 \%$ level of confidence.

| Level of confidence | 90 | 95 | 98 | 99 |
| :---: | :---: | :---: | :---: | :---: |
| $Z_{\frac{\alpha}{2}}$ | 1.64 | 1.96 | 2.33 | 2.58 |

c) Given the following data:

| $\mathbf{X}$ | 9 | 11 | 9 | 14 | 14 | 13 | 16 | 18 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Y}$ | 12 | 18 | 18 | 20 | 20 | 22 | 24 | 26 |

i. Obtain the two regression equations
ii. Obtain the value of the coefficient of correlation

Q7) Any two from (a) or (b) or (c) (5x2) = 10 Marks
a) Find the probability that
i. The sum of digits on a pair of dice is equal to 8 .
ii. The product of digits obtained on tossing of two balanced dice is a perfect square.
d) For following distribution compute inter-quartile range

| Marks | No. of <br> Students |
| :---: | :---: |
| $20-30$ | 4 |
| $30-40$ | 12 |
| $40-50$ | 18 |
| $50-60$ | 28 |
| $60-70$ | 19 |
| $70-80$ | 14 |
| $80-90$ | 5 |

e) Calculate the three coefficient of multiple correlation using the following coefficient as inputs: $r_{12}=0.70, r_{13}=0.61, r_{23}=0.40$

