


|  | F-table of Critical Values of $\alpha=0.05$ for F(df1, df2) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | DF1=1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 12 | 15 | 20 | 24 | 30 | 40 | 60 | 120 | $\infty$ |
| DF2 $=1$ | 161.45 | 199.50 | 215.71 | 224.58 | 230.16 | 233.99 | 236.77 | 238.88 | 240.54 | 241.88 | 243.91 | 245.95 | 248.01 | 249.05 | 250.10 | 251.14 | 252.20 | 253.25 | 254.31 |
| 2 | 18.51 | 19.00 | 19.16 | 19.25 | 19.30 | 19.33 | 19.35 | 19.37 | 19.38 | 19.40 | 19.41 | 19.43 | 19.45 | 19.45 | 19.46 | 19.47 | 19.48 | 19.49 | 19.50 |
| 3 | 10.13 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.89 | 8.85 | 8.81 | 8.79 | 8.74 | 8.70 | 8.66 | 8.64 | 8.62 | 8.59 | 8.57 | 8.55 | 8.53 |
| 4 | 7.71 | 6.94 | 6.59 | 6.39 | 6.26 | 6.16 | 6.09 | 6.04 | 6.00 | 5.96 | 5.91 | 5.86 | 5.80 | 5.77 | 5.75 | 5.72 | 5.69 | 5.66 | 5.63 |
| 5 | 6.61 | 5.79 | 5.41 | 5.19 | 5.05 | 4.95 | 4.88 | 4.82 | 4.77 | 4.74 | 4.68 | 4.62 | 4.56 | 4.53 | 4.50 | 4.46 | 4.43 | 4.40 | 4.37 |
| 6 | 5.99 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.21 | 4.15 | 4.10 | 4.06 | 4.00 | 3.94 | 3.87 | 3.84 | 3.81 | 3.77 | 3.74 | 3.70 | 3.67 |
| 7 | 5.59 | 4.74 | 4.35 | 4.12 | 3.97 | 3.87 | 3.79 | 3.73 | 3.68 | 3.64 | 3.57 | 3.51 | 3.44 | 3.41 | 3.38 | 3.34 | 3.30 | 3.27 | 3.23 |
| 8 | 5.32 | 4.46 | 4.07 | 3.84 | 3.69 | 3.58 | 3.50 | 3.44 | 3.39 | 3.35 | 3.28 | 3.22 | 3.15 | 3.12 | 3.08 | 3.04 | 3.01 | 2.97 | 2.93 |
| 9 | 5.12 | 4.26 | 3.86 | 3.63 | 3.48 | 3.37 | 3.29 | 3.23 | 3.18 | 3.14 | 3.07 | 3.01 | 2.94 | 2.90 | 2.86 | 2.83 | 2.79 | 2.75 | 2.71 |
| 10 | 4.96 | 4.10 | 3.71 | 3.48 | 3.33 | 3.22 | 3.14 | 3.07 | 3.02 | 2.98 | 2.91 | 2.85 | 2.77 | 2.74 | 2.70 | 2.66 | 2.62 | 2.58 | 2.54 |
| 11 | 4.84 | 3.98 | 3.59 | 3.36 | 3.20 | 3.09 | 3.01 | 2.95 | 2.90 | 2.85 | 2.79 | 2.72 | 2.65 | 2.61 | 2.57 | 2.53 | 2.49 | 2.45 | 2.40 |
| 12 | 4.75 | 3.89 | 3.49 | 3.26 | 3.11 | 3.00 | 2.91 | 2.85 | 2.80 | 2.75 | 2.69 | 2.62 | 2.54 | 2.51 | 2.47 | 2.43 | 2.38 | 2.34 | 2.30 |
| 13 | 4.67 | 3.81 | 3.41 | 3.18 | 3.03 | 2.92 | 2.83 | 2.77 | 2.71 | 2.67 | 2.60 | 2.53 | 2.46 | 2.42 | 2.38 | 2.34 | 2.30 | 2.25 | 2.21 |
| 14 | 4.60 | 3.74 | 3.34 | 3.11 | 2.96 | 2.85 | 2.76 | 2.70 | 2.65 | 2.60 | 2.53 | 2.46 | 2.39 | 2.35 | 2.31 | 2.27 | 2.22 | 2.18 | 2.13 |
| 15 | 4.54 | 3.68 | 3.29 | 3.06 | 2.90 | 2.79 | 2.71 | 2.64 | 2.59 | 2.54 | 2.48 | 2.40 | 2.33 | 2.29 | 2.25 | 2.20 | 2.16 | 2.11 | 2.07 |
| 16 | 4.49 | 3.63 | 3.24 | 3.01 | 2.85 | 2.74 | 2.66 | 2.59 | 2.54 | 2.49 | 2.42 | 2.35 | 2.28 | 2.24 | 2.19 | 2.15 | 2.11 | 2.06 | 2.01 |
| 17 | 4.45 | 3.59 | 3.20 | 2.96 | 2.81 | 2.70 | 2.61 | 2.55 | 2.49 | 2.45 | 2.38 | 2.31 | 2.23 | 2.19 | 2.15 | 2.10 | 2.06 | 2.01 | 1.96 |
| 18 | 4.41 | 3.55 | 3.16 | 2.93 | 2.77 | 2.66 | 2.58 | 2.51 | 2.46 | 2.41 | 2.34 | 2.27 | 2.19 | 2.15 | 2.11 | 2.06 | 2.02 | 1.97 | 1.92 |
| 19 | 4.38 | 3.52 | 3.13 | 2.90 | 2.74 | 2.63 | 2.54 | 2.48 | 2.42 | 2.38 | 2.31 | 2.23 | 2.16 | 2.11 | 2.07 | 2.03 | 1.98 | 1.93 | 1.88 |
| 20 | 4.35 | 3.49 | 3.10 | 2.87 | 2.71 | 2.60 | 2.51 | 2.45 | 2.39 | 2.35 | 2.28 | 2.20 | 2.12 | 2.08 | 2.04 | 1.99 | 1.95 | 1.90 | 1.84 |
| 21 | 4.32 | 3.47 | 3.07 | 2.84 | 2.68 | 2.57 | 2.49 | 2.42 | 2.37 | 2.32 | 2.25 | 2.18 | 2.10 | 2.05 | 2.01 | 1.96 | 1.92 | 1.87 | 1.81 |
| 22 | 4.30 | 3.44 | 3.05 | 2.82 | 2.66 | 2.55 | 2.46 | 2.40 | 2.34 | 2.30 | 2.23 | 2.15 | 2.07 | 2.03 | 1.98 | 1.94 | 1.89 | 1.84 | 1.78 |
| 23 | 4.28 | 3.42 | 3.03 | 2.80 | 2.64 | 2.53 | 2.44 | 2.37 | 2.32 | 2.27 | 2.20 | 2.13 | 2.05 | 2.01 | 1.96 | 1.91 | 1.86 | 1.81 | 1.76 |
| 24 | 4.26 | 3.40 | 3.01 | 2.78 | 2.62 | 2.51 | 2.42 | 2.36 | 2.30 | 2.25 | 2.18 | 2.11 | 2.03 | 1.98 | 1.94 | 1.89 | 1.84 | 1.79 | 1.73 |
| 25 | 4.24 | 3.39 | 2.99 | 2.76 | 2.60 | 2.49 | 2.40 | 2.34 | 2.28 | 2.24 | 2.16 | 2.09 | 2.01 | 1.96 | 1.92 | 1.87 | 1.82 | 1.77 | 1.71 |
| 26 | 4.23 | 3.37 | 2.98 | 2.74 | 2.59 | 2.47 | 2.39 | 2.32 | 2.27 | 2.22 | 2.15 | 2.07 | 1.99 | 1.95 | 1.90 | 1.85 | 1.80 | 1.75 | 1.69 |
| 27 | 4.21 | 3.35 | 2.96 | 2.73 | 2.57 | 2.46 | 2.37 | 2.31 | 2.25 | 2.20 | 2.13 | 2.06 | 1.97 | 1.93 | 1.88 | 1.84 | 1.79 | 1.73 | 1.67 |
| 28 | 4.20 | 3.34 | 2.95 | 2.71 | 2.56 | 2.45 | 2.36 | 2.29 | 2.24 | 2.19 | 2.12 | 2.04 | 1.96 | 1.91 | 1.87 | 1.82 | 1.77 | 1.71 | 1.65 |
| 29 | 4.18 | 3.33 | 2.93 | 2.70 | 2.55 | 2.43 | 2.35 | 2.28 | 2.22 | 2.18 | 2.10 | 2.03 | 1.94 | 1.90 | 1.85 | 1.81 | 1.75 | 1.70 | 1.64 |
| 30 | 4.17 | 3.32 | 2.92 | 2.69 | 2.53 | 2.42 | 2.33 | 2.27 | 2.21 | 2.16 | 2.09 | 2.01 | 1.93 | 1.89 | 1.84 | 1.79 | 1.74 | 1.68 | 1.62 |
| 40 | 4.08 | 3.23 | 2.84 | 2.61 | 2.45 | 2.34 | 2.25 | 2.18 | 2.12 | 2.08 | 2.00 | 1.92 | 1.84 | 1.79 | 1.74 | 1.69 | 1.64 | 1.58 | 1.51 |
| 60 | 4.00 | 3.15 | 2.76 | 2.53 | 2.37 | 2.25 | 2.17 | 2.10 | 2.04 | 1.99 | 1.92 | 1.84 | 1.75 | 1.70 | 1.65 | 1.59 | 1.53 | 1.47 | 1.39 |
| 120 | 3.92 | 3.07 | 2.68 | 2.45 | 2.29 | 2.18 | 2.09 | 2.02 | 1.96 | 1.91 | 1.83 | 1.75 | 1.66 | 1.61 | 1.55 | 1.50 | 1.43 | 1.35 | 1.25 |


| t Distribution |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\alpha$ |  |  |  |  |  |  |
| Degrees of Erecedom | $\begin{gathered} 005 \\ \text { (one tail) } \\ \text {. 01 } \\ \text { (two tails) } \end{gathered}$ | $\begin{gathered} 01 \\ \text { (one tail) } \\ 02 \\ \text { (two tails) } \end{gathered}$ | $\begin{gathered} .025 \\ \text { (one tail) } \\ .05 \\ \text { (two tails) } \end{gathered}$ | $\begin{gathered} 05 \\ \text { (one tail) } \\ .10 \\ \text { (two tails) } \end{gathered}$ | $\begin{gathered} 10 \\ \text { (one tail) } \\ 20 \\ \text { (two tails) } \end{gathered}$ | $\begin{gathered} 25 \\ \text { (one tail) } \\ 50 \\ \text { (two tails) } \end{gathered}$ |
| $\begin{aligned} & 1 \\ & 2 \\ & 3 \\ & 4 \\ & 5 \end{aligned}$ | $\begin{array}{r} 63.657 \\ 9.925 \\ 5.841 \\ 4.604 \\ 4.032 \end{array}$ | $\begin{array}{r} 31.821 \\ 6.965 \\ 4.541 \\ 3.747 \\ 3.365 \end{array}$ | $\begin{array}{r} 12.706 \\ 4.303 \\ 3.182 \\ 2.776 \\ 2.571 \end{array}$ | $\begin{aligned} & 6.314 \\ & 2.920 \\ & 2.353 \\ & 2.132 \\ & 2.015 \end{aligned}$ | $\begin{aligned} & 3.078 \\ & 1.886 \\ & 1.638 \\ & 1.533 \\ & 1.476 \end{aligned}$ | $\begin{array}{r} 3.000 \\ 816 \\ 765 \\ 741 \\ 727 \end{array}$ |
| $\begin{array}{r} 6 \\ 7 \\ 8 \\ 9 \\ 10 \end{array}$ | $\begin{aligned} & 3.707 \\ & 3.500 \\ & 3.355 \\ & 3.250 \\ & 3.169 \end{aligned}$ | $\begin{aligned} & 2.143 \\ & 2.998 \\ & 2.896 \\ & 2.821 \\ & 2.764 \end{aligned}$ | $\begin{aligned} & 2.447 \\ & 2.365 \\ & 2.306 \\ & 2.262 \\ & 2.228 \end{aligned}$ | $\begin{aligned} & 1.943 \\ & 1.895 \\ & 1.860 \\ & 1.833 \\ & 1812 \end{aligned}$ | $\begin{aligned} & 1.440 \\ & 1.415 \\ & 1.397 \\ & 1.383 \\ & 1.372 \end{aligned}$ | $\begin{aligned} & .718 \\ & .711 \\ & .706 \\ & .703 \\ & .700 \end{aligned}$ |
| $\begin{aligned} & 11 \\ & 12 \\ & 13 \\ & 14 \\ & 15 \end{aligned}$ | $\begin{aligned} & 3.106 \\ & 3.054 \\ & 3.012 \\ & 2.977 \\ & 2.547 \end{aligned}$ | $\begin{aligned} & 2.718 \\ & 2.681 \\ & 2.650 \\ & 2.625 \\ & 2.602 \end{aligned}$ | $\begin{aligned} & 2.201 \\ & 2.179 \\ & 2.160 \\ & 2.145 \\ & 2.132 \end{aligned}$ | $\begin{aligned} & 1.796 \\ & 1.782 \\ & 1.771 \\ & 1.761 \\ & 1.753 \end{aligned}$ | $\begin{aligned} & 1.363 \\ & 1.356 \\ & 1.350 \\ & 1.345 \\ & 1.341 \end{aligned}$ | $\begin{aligned} & 697 \\ & 696 \\ & 6994 \\ & 692 \\ & 691 \end{aligned}$ |
| $\begin{aligned} & 16 \\ & 17 \\ & 18 \\ & 19 \\ & 20 \end{aligned}$ | 2.921 2.898 2.878 2.861 2.845 | $\begin{aligned} & 2.584 \\ & 2.587 \\ & 2.552 \\ & 2.540 \\ & 2.528 \end{aligned}$ | $\begin{aligned} & 2.120 \\ & 2.110 \\ & 2.101 \\ & 2.093 \\ & 2.086 \end{aligned}$ | $\begin{aligned} & 1.746 \\ & 1.740 \\ & 1.734 \\ & 1.729 \\ & 1.725 \end{aligned}$ | $\begin{aligned} & 1.337 \\ & 1.333 \\ & 1.330 \\ & 1.328 \\ & 1.325 \end{aligned}$ | $\begin{aligned} & 690 \\ & 689 \\ & 688 \\ & 688 \\ & 687 \end{aligned}$ |
| 21 22 23 24 25 | 2.831 2.819 2.807 2.797 2.787 | $\begin{aligned} & 2.518 \\ & 2.508 \\ & 2.500 \\ & 2.492 \\ & 2.485 \end{aligned}$ | $\begin{aligned} & 2.080 \\ & 2.074 \\ & 2.069 \\ & 2.064 \\ & 2.060 \end{aligned}$ | $\begin{aligned} & 1.721 \\ & 1.717 \\ & 1.714 \\ & 1.711 \\ & \hline 1.708 \end{aligned}$ | $\begin{aligned} & 1323 \\ & 1321 \\ & 1320 \\ & 1.318 \\ & 1.316 \end{aligned}$ | . 686 <br> 686 <br> 685 <br> 685 <br> .64 |
| $\begin{array}{r} 26 \\ 27 \\ 28 \\ 29 \\ \text { Large ( } 2) \end{array}$ | 2.779 2.771 2.763 2.756 2.575 | 2.479 2.473 2.467 2.462 2.327 | $\begin{aligned} & 2.056 \\ & 2.052 \\ & 2.045 \\ & 2.045 \\ & 1.560 \end{aligned}$ | 1.706 1.703 1.701 1.699 1.645 | $\begin{aligned} & 1.315 \\ & 1.314 \\ & 1.313 \\ & 1.311 \\ & 1.282 \end{aligned}$ | . 684 <br> 684 <br> .683 <br> .683 <br> .675 |

## Critical values of the Chi-square distribution with d degrees of freedom

| $d$ | Probability of exceeding the critical value |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.05 | 0.01 | 0.001 | $d$ | 0.05 | 0.01 | 0.001 |
| 1 | 3.841 | 6.635 | 10.828 | 11 | 19.675 | 24.725 | 31.264 |
| 2 | 5.991 | 9.210 | 13.816 | 12 | 21.026 | 26.217 | 32.910 |
| 3 | 7.815 | 11.345 | 16.266 | 13 | 22.362 | 27.688 | 34.528 |
| 4 | 9.488 | 13.277 | 18.467 | 14 | 23.685 | 29.141 | 36.123 |
| 5 | 11.070 | 15.086 | 20.515 | 15 | 24.996 | 30.578 | 37.697 |
| 6 | 12.592 | 16.812 | 22.458 | 16 | 26.296 | 32.000 | 39.252 |
| 7 | 14.067 | 18.475 | 24.322 | 17 | 27.587 | 33.409 | 40.790 |
| 8 | 15.507 | 20.090 | 26.125 | 18 | 28.869 | 34.805 | 42.312 |
| 9 | 16.919 | 21.666 | 27.877 | 19 | 30.144 | 36.191 | 43.820 |
| 10 | 18.307 | 23.209 | 29.588 | 20 | 31.410 | 37.566 | 45.315 |

INTRODUCTION TO POPULATION GENETICS, Table D. 1
© 2013 Sinauer Associates, Inc.

